

RUTGERS UNIVERSITY
DEPARTMENT OF STATISTICS AND BIostatISTICS
HILL CENTER ROOM 501, BUSCH CAMPUS, PISCATAWAY
www.stat.rutgers.edu

Seminar

Speaker: Vladislav Vysotsky, University of Delaware
Title: On probability that an integrated random walk stays positive
Date: Wednesday October 7, 2009
Time: 3:20 P.M.
Place: 552 Hill Center

Abstract

Let S_n be a centered random walk, and define the new sequence $\sum_{i=1}^n S_i$, which we call the *integrated random walk*. We are interested in the asymptotics of

$$p_N := P\left\{\min_{1 \leq k \leq N} \sum_{i=1}^k S_i \geq 0\right\}$$

as $N \rightarrow \infty$. Sinai (1992) proved that $p_N \asymp N^{-1/4}$ if S_n is a simple random walk. Our results show that p_N has the same asymptotics for some other types of random walks, including Laplace walk. We also prove that $p_N \leq cN^{-1/4}$ for any centered lattice walks and certain continuous walks.